## P XXX/00 Terms and definitions used with Thermodyn

<b>Free energy equation:</b> $\Delta G_r = \Delta H_r - T \cdot \Delta S_r$			
<b>Equilibrium equation:</b> $\Delta G_r = 0$			
$\Delta G_r^0 = -R \cdot T \cdot \ln K^0 \qquad \Delta G_r^0 = \sum v_j G f_{P_j}^0 - \sum v_i G f_{S_i}^0$	(2)		
or			
$\mathbf{K}^{0} = \exp\left[\frac{-\Delta \mathbf{G}_{\mathrm{r}}^{0}}{\mathbf{R} \cdot \mathbf{T}}\right]$			
<b>Disequilibrium equation:</b> $\Delta G_r < 0$			
$\Delta G_r = \Delta G_r^0 + R \cdot T \cdot \ln Q$ or	(3)		
$\Delta G_{\rm r} = \mathbf{R} \cdot \mathbf{T} \cdot \ln \frac{\mathbf{Q}}{\mathbf{K}^0} \qquad \qquad \frac{\mathbf{Q}}{\mathbf{K}^0} < 1$			
or			
$Q = K^{0} \cdot \exp\left[\frac{\Delta G_{r}}{R \cdot T}\right]$			
or			
$Q = K^{0} \cdot \exp\left[\frac{-E \cdot n \cdot F}{R \cdot T}\right]$			
Influence of temperature changes on equilibrium equation: $\Delta G_{r,T_{act}}^{0} = \Delta G_{r,T_{ref}}^{0} \cdot \frac{T_{act}}{T_{ref}} + \Delta H_{r,T_{ref}}^{0} \cdot \frac{T_{ref} - T_{act}}{T_{ref}}$			
Influence of temperature changes on equilibrium constant: $pK_{T_{act}}^{0} = pK_{T_{ref}}^{0} + \frac{\Delta H_{r,T_{ref}}^{0}}{2.3026 \cdot R} \cdot \frac{T_{ref} - T_{act}}{T_{ref} \cdot T_{act}}$			

Influence of pH-changes on equilibrium equation:	
$\Delta G_{r}^{0'} = \Delta G_{r}^{0} - 2.3026 \cdot R \cdot T \cdot q \cdot pH_{act}$	(4)
Influence of pH-changes on disequilibrium equation:	
$\Delta G_{r} = \Delta G_{r}^{0} + 2.3026 \cdot R \cdot T \cdot \left( \log Q_{neq} - q \cdot pH_{act} \right)$	(5)
or	
$\Delta G_{r} = 2.3026 \cdot R \cdot T \cdot \left( pK^{0} + \log Q_{neq} - q \cdot pH_{act} \right)$	(5)

ETH Zürich, Biogeosciences at the Department of Earth Sciences and University of Zürich, Microbial Ecology Group. Address: Sonneggstreet 5, 8092 Zürich, mail to: kurt.hanselmann@erdw.ethz.ch

## **Influence of changes in solute concentrations on solubility products:** (follows from equilibrium equation):

 $pK_{s} = pK_{s}^{0} - \log (\prod_{j} f_{j}^{v_{j}})$ or

 $pK_{s}^{'} = pK_{s}^{0'} + \sum_{j} \frac{v_{j} \cdot A \cdot z_{j}^{2} \cdot \sqrt{I}}{1 + a_{j} \cdot B \cdot \sqrt{I}}$ 

**Influence of changes in solute concentrations on precipitation-dissolution reactions:** (follows from disequilibrium equation):

$\Delta G_{r} = R \cdot T \cdot \ln \frac{IAP}{K_{s}}$	dissolution if	$\Delta G_r < 0$ or	$\frac{\text{IAP}}{\text{K}_{s}} < 1$
	precipitation if	$\Delta G_r > 0$ or	$\frac{\text{IAP}}{\text{K}_{s}} > 1$
saturatio	on equilibrium if	$\Delta G_r = 0$ or	$\frac{\text{IAP}}{\text{K}_{\text{S}}} = 1$

Influence of changes in pH, I (ionic strength) and T on the species composition of the carbonatebicarbonate-carbonic acid equilibrium:

$$\begin{bmatrix} CO_3^{2-} \end{bmatrix} = \begin{bmatrix} C_T \end{bmatrix} \cdot \frac{K_{a_1} \cdot K_{a_2}}{10^{-2pH} + K_{a_1} \cdot 10^{-pH} + K_{a_1} \cdot K_{a_2}}$$
$$\begin{bmatrix} HCO_3^{-} \end{bmatrix} = \begin{bmatrix} C_T \end{bmatrix} \cdot \frac{K_{a_1} \cdot 10^{-pH}}{10^{-2pH} + K_{a_1} \cdot 10^{-pH} + K_{a_1} \cdot K_{a_2}}$$
$$\begin{bmatrix} H_2CO_3 \end{bmatrix} = \begin{bmatrix} C_T \end{bmatrix} \cdot \frac{10^{-2pH}}{10^{-2pH} + K_{a_1} \cdot 10^{-pH} + K_{a_1} \cdot K_{a_2}}$$

Influence of changes in solute concentrations on disequilibrium redox potentials:

$$E = \frac{-\Delta G_r}{n \cdot F}$$
or
$$E = \frac{-\Delta G_r^0}{n \cdot F} - \frac{R \cdot T}{n \cdot F} \cdot \ln Q \quad \text{and since } \frac{-\Delta G_r^0}{n \cdot F} = E^0, \text{ and } \Delta G_r^0 = -R \cdot T \cdot \ln K^0 \quad (6)$$

$$E = E^0 - \frac{R \cdot T}{n \cdot F} \cdot \ln Q$$
or
$$E = \frac{R \cdot T}{n \cdot F} \cdot \ln \frac{K^0}{Q}$$

## Influence of changes in pH on standard redox potentials:

$$E^{0'} = E^{0} - \frac{2.3026 \cdot R \cdot T}{F} \cdot \frac{q}{n} \cdot pH$$
(4)  
Influence of changes in pH and/or solute concentrations on disequilibrium redox potential:  

$$E = -\frac{\Delta G_{r}^{0}}{n \cdot F} - \frac{2.3026 \cdot R \cdot T}{n \cdot F} \cdot \left( \log Q'_{red/ox} - q \cdot pH_{act} \right)$$
(8),(7),(4)  
or  

$$E = E^{0} - \frac{2.3026 \cdot R \cdot T}{n \cdot F} \cdot \left( \log Q'_{red/ox} - q \cdot pH_{act} \right)$$
  
or  

$$E = \frac{2.3026 \cdot R \cdot T}{n \cdot F} \cdot \left( pK^{0} + \log Q'_{red/ox} - q \cdot pH_{act} \right)$$

Influence of changes in solute concentrations or/and pH on disequilibrium electron activity:  $pe = \frac{1}{n} \cdot \log K^{0} - \frac{q}{n} \cdot pH - \frac{1}{n} \cdot \log Q'_{red/ox}$ (7), (4), (9)

## Notes and explanations

(1) See list of abbreviations for meaning of terms.

(2) 
$$K^{0} \stackrel{c}{=} K_{eq} = \frac{\prod_{j} \{P_{jeq}\}^{v_{j}}}{\prod_{i} \{S_{ieq}\}^{v_{i}}}$$
  
(3)  $Q = \frac{\prod_{j} \{P_{jneq}\}^{v_{j}}}{\prod_{i} \{S_{ineq}\}^{v_{i}}}$ 

(4) q is – for  $H^+$ -consuming and + for  $H^+$ -producing reactions respectively.

(5) From 
$$Q = \frac{\prod_{j}^{q} \left\{ P_{jneq}^{i} \right\}^{v_{j}} \cdot \left\{ H^{+} \right\}^{q}}{\prod_{i}^{q} \left\{ S_{ineq}^{i} \right\}^{v_{i}}} = Q_{neq}^{i} \cdot \left\{ H^{+} \right\}^{q}}$$
 follows:  $Q_{neq}^{i} = \frac{Q}{\left\{ H^{+} \right\}^{q}}$   
(6)  $Q = \frac{\prod_{j}^{q} \left\{ P_{jred}^{i} \right\}^{v_{j}}}{\prod_{i}^{q} \left\{ S_{iox}^{i} \right\}^{v_{i}}}$   
(7) From  $Q = \frac{\prod_{j}^{q} \left\{ P_{jred}^{i} \right\}^{v_{j}}}{\prod_{i}^{q} \left\{ S_{iox}^{i} \right\}^{v_{i}} \cdot \left\{ H^{+} \right\}^{q} \cdot \left\{ e^{-} \right\}^{n}} = Q_{red/ox}^{i} \cdot \left\{ H^{+} \right\}^{-q} \cdot \left\{ e^{-} \right\}^{-n}}$  follows:  $Q_{red/ox}^{i} = Q \cdot \left\{ H^{+} \right\}^{q} \cdot \left\{ e^{-} \right\}^{n}}$   
(8) Electrons which are given off by oxidation half - reactions are assigned a negative sign, electrons which are consumed by reduction half - reactions have a positive sign.  
(9) n is always + in the pe - formalism.